



## Editorial

# 2nd Special issue on matrix computations and statistics

A number of interesting and important ideas have resulted from the relationship between matrix computations and statistics. Well-known examples include the solution of least-squares problems, computation of the singular value decomposition and its generalizations, estimation of principal components, computation of canonical correlations, several cluster analysis algorithms, and the solution of total least-squares problems.

Computational statistics and data analysis has published papers in matrix computations and statistics (for instance, Doornik and Ooms, 2003; Eldén, 2004; Foschi et al., 2003; Kawai, 2004; Molinari et al., 2004; Pollock, 2003; Wilkinson and Yeung, 2004) and encourages submissions in this area. A previous special issue on this area featured papers on multidimensional scaling, an application to web search engines, an algorithm for seemingly unrelated regression models, an error measurement model for motion analysis, and a survey on alternating least-squares problems (Chang and Paige, 2002; Dhillon et al., 2002; Doornik and O'Brien, 2002; Erbay et al., 2002; Fodor and Kamath, 2002; Foschi and Kontoghiorghes, 2002; Genton and Gorsich, 2002; Georgiou et al., 2002; He et al., 2002; Kiers, 2002; Kukush et al., 2002; Malone et al., 2002; Vigneau and Qannari, 2002).

This second special issue on matrix computations and statistics continues in this direction. It contains topics such as new data analysis models, fast computational methods, and theoretical developments using matrix computations in statistics: a new model for principal components of binary data, high-speed smoothing for large grids, a theoretical and practical comparison of canonical correlation analysis and Procrustes analysis, a generalization of constrained correspondence analysis, a new generalization of total least squares, a study of the conditions for uniqueness of estimates in three-way models, a study of the use of the modified Leverrier–Faddeev algorithm to the spectral decomposition of symmetric block-circulant matrices, and a sensitivity analysis of the Strain criterion for multidimensional scaling.

Several papers developed matrix computational algorithms that were inspired by statistical applications. Li (2004) discusses the definition and application of sign eigenvectors. Sign eigenanalysis can be applied to the development of statistical inference procedures in the  $\ell_1$  norm. Dax (2004) presents a method for solving a system of linear inequalities  $\mathbf{Ax} \geq \mathbf{b}$ . This problem is a  $\ell_1$  minimization problem or  $\ell_1$  regression problem. Gower (2004)

applies the Leverrier–Faddeev algorithm for deriving the algebraic structure of matrices to find the singular value decomposition of block-circulant matrices. Chang (2004) proposes a method for the efficient computation of Huber’s M-estimator. Updating/downdating methods for matrix factorizations and special structure of the problem are exploited to make the algorithm efficient.

Aspects of dimension reduction are considered in four other papers in this volume. Trendafilov and Jolliffe (2004) consider a projected gradient approach to a principal component problem where the principal components satisfy a one-norm constraint. Li and Zha (2004) use a mixture of Poisson distributions to model document classification and word clustering in term-document models. The parameters are regularized by imposing a clustering strategy on the set of words. Yamada et al. (2004) discuss mixed-level supersaturated design. This is a first step in reducing the number of factors in a large experiment. De Leeuw (2004) combines ideas from latent structure analysis with principal component analysis and multiple component analysis for binary data. The algorithms they propose can be fitted efficiently to large matrices.

Canonical correlations were among the themes of three papers. Gardner et al. (2004) synthesize canonical variate analysis, Procrustes analysis, and generalized canonical correlation. Using a data mining example consisting of 1425 samples, they isolate a four class structure using generalized canonical correlation, and use its synthesis with canonical variate analysis to discern the structure of the data in more detail. Takhane et al. (2004) develop a method for generalized constrained canonical correlation analysis based upon two orthogonal decomposition of projectors. This work improves upon previous work by two of the authors on a related technique.

Two papers concern scaling in a model and lead to solving an optimization problem. Lewis and Trosset (2004) offer a perturbation analysis of the strain criterion of multidimensional scaling. Their analysis builds gradients and Hessians of the appropriate objective functions from eigenvalue perturbation theory. Markovsky et al. (2004) develop a version of the total least squares (or errors-in-variables) model. This model allows for more general covariance structures for incorporating certain kinds of scaling in the total least-squares problem.

A final set of papers concerns the multidimensional representation of data. Eilers et al. (2004) present what they call a P-spline approach to multidimensional grids. A smooth multidimensional surface is constructed out of tensor products of B-splines. They approach this problem in a manner that reduces the memory required and works for any number of dimensions. Stegeman and Ten Berge (2004) analyze the Condecomp/Parafac method for component analysis of three-way arrays. They disprove a conjecture about this approach. Evangelaras and Koukouvinos (2004) show how the theory of Gröbner bases allow one to identify estimable effects of the factors in an experimental design.

As can be seen from this special issue and the papers that CSDA has already published in this area, the interaction between matrix computations and statistics will continue to be a rich and intellectually challenging area of research.

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