Performance Analysis of Communications & Radar Coexistence in a Covert UWB OSA System

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Abstract—Far-field target detection, multi-sensor communications, and security are essential requirements of first-emergency networks. A radar-communications system is a potential opportunistic spectrum access (OSA) solution, harnessing the co-existing advantages of radio detection and ranging (RADAR), and wireless communications. A multi-functional waveform has been designed, by embedding an Orthogonal Frequency Division Multiplexing (OFDM) signal within a spectrally notched ultra-wideband (UWB) random noise waveform. Extending that development, this paper analyzes the waveform's Bit-Error-Rate (BER) and Ambiguity Function (AF) formulations to demonstrate its OSA ability, that offers reliable multi-user communications, and high range and Doppler resolution in target detection. We further conclude that up to 30% of the available UWB bandwidth can be simultaneously utilized for concealed data communications without adversely affecting radar performance or its physical layer covertness.

I. INTRODUCTION

The capability of far-field or through-the-wall sensing of phenomenon and communicating it to a command center is a prime requirement for first-emergency networks. UWB technology, a promising avenue, not only for through-the-wall radio detection and ranging (radar) [1], but also for its coexistence with wireless communications [2], is therefore, a viable solution to potentially exploit the coexisting advantages of radar and communications.

On the other hand, OFDM has gained popularity in the dynamic spectrum access arena as a prime candidate for modulation in OSA networks. Ref. [3] presents an OSA solution where the OFDM waveform as the secondary user, is sculpted to enable coexistence with a primary user. We extend this horizon towards a covert OSA solution, by working with OFDM's noise-like spectrum behavior. Our approach is to spectrally sculpt the random noise waveform of a UWB Noise Radar (the primary user), to spectrally embed OFDM based data symbols (the secondary user). This generates a covert communication platform can be formed between the individual noise radars. With this possibility to have data communication within the same spectrum as the radars transmit signal, a substantial increase in capacity and bandwidth efficiency can be achieved. The physical layer (PHY) design of such an point-to-point radar-communications system, the UWB Noise-OFDM Radar, has been analyzed in [4]. It is a hybrid radar-communications architecture wherein both functionalities are contained, viz. UWB noise waveform for radar operation and OFDM waveform for communications operation.

Establishing a multi-user ad hoc network among such radars, can lead to data being gathered from the individual radars to be collectively processed and transformed into useful information for enhanced situational awareness. This paper, therefore, extends the UWB Noise-OFDM radar proposed in [4] to demonstrate its ability of multi-user covert communication between the radars, concurrent with the ability to perform radar operations like high-resolution target detection and ranging. The two important parameters we investigate for this performance analysis are the BER reliability measure for communications, and the AF resolution measure for radar operations [5].

Compared to generic multi-static or netted radar systems [6], the UWB Noise-OFDM radar is distinct OSA solution where the same transmit signal is simultaneously used for both radar and communication operations, and is inherently secure. In [7], a comparable dual-system is presented which uses UWB OFDM pulses for radar and communication. While this is indeed a viable alternative, immunity from detection requires random frequency hopping. Furthermore, the UWB OFDM pulses show greater range side-lobes compared to Gaussian pulses and the communication system requires full synchronization between the platforms. Further examining the existing UWB radar-communication systems, we observed that they are either not multi-radar capable [8], or are easily jammed open communication systems [7]. In contrast, we present a multi-functional UWB netted radar with better coexistence of radar and communication abilities, along with inherent transmit waveform covertness and multi-radar capability. Overall, the primary contributions of this work are:

- We demonstrate that a reliable multi-user communication platform exists in our system, which can form the physical layer for a wireless radar network. This is seen from our simulations results, which shows a BER value better than 1×10^{-4} for an SNR of 9 dB.
- By formulating and deriving the AF for the radar part of the Noise-OFDM Radar and comparing with the AF of a conventional Noise Radar, we show that if the fragmented gap is less than 30%, then range and Doppler resolution i.e., the radar performance, is essentially unaffected.

By observing that the above two properties are *due* to the same composite Noise-OFDM signal, it is straight-forward to understand the coexistence of communications and radar.

II. BACKGROUND: SYSTEM DESIGN

The UWB Noise-OFDM Radars system architecture is briefly described in this section. Every device performs two specific functions: (1) radar specific operations such as target detection, ranging, velocity (Doppler) estimation and tracking, and (2) data-communication with other radar sensors and the centralized command center.

A. Transmit Component

Fig. 1. UWB Noise-OFDM Radar: Transmit Component Architecture.

A noise generator produces a signal with a Gaussian amplitude distribution and approximately constant power spectral density (PSD). This signal is filtered in a Band-pass Filter (BPF) to generate a band-limited UWB noise signal within a range of (f_1, f_2) GHz, as shown in Fig. 1. Such a band-pass Gaussian process with bandwidth β and centered at some frequency f_o , where $f_o > \beta/2$, can be expressed as

$$X_G(t) = \frac{1}{2} [u(t)\exp(j2\pi f_o t) + u^*(t)\exp(-j2\pi f_o t)], \quad (1)$$

where $u(t) = X_c + jX_s$ is the complex envelope and $*$ indicates the complex conjugation operation. In our simulations, we used a 1-2 GHz frequency range of operation. For our system therefore, $f_o = 1.5$ GHz, $f_1 = 1$ GHz, and $f_2 = 2$ GHz. This is a UWB signal by definition since its fractional bandwidth (β/f_o) is greater than 0.25. This band-limited noise signal is then notch-filtered within the narrower range of 1.2-1.3 GHz (in general, this could be done over any range suitable for the application). The radar system uses the full 1-2 GHz band, while the intra-sensor communications is achieved by utilizing the 1.2-1.3 GHz sub-band. The Gaussian process $X_N(t)$ in the notched band, has bandwidth β_n and is centered at frequency f_n , such that $f_o - \beta/2 < f_n < f_o + \beta/2$. We use a random binary number generator to generate test data. In general, this would be the target data that the radar collects, or any other information it wishes to communicate to other radars in its vicinity. Because we want to hide this data within noise, and since an OFDM waveform's spectral characteristics closely mimic that of white noise, we map this data onto OFDM subcarriers to generate the OFDM symbols. A pass-band real OFDM signal with a communication carrier f_n , can be represented as [9]:

$$X_D(t) = \frac{1}{2} [s(t)\exp(j2\pi f_n t) + s^*(t)\exp(-j2\pi f_n t)], \quad (2)$$

Fig. 2. Spectrum: (a) Secondary user: OFDM Signal (b) Primary user: Band-limited UWB Noise (c) UWB Notched Noise and (d) OSA: UWB Noise-OFDM spectrum. Comparing (b) and (d), transmit waveform (d) also appears random & noise-like, similar to (b), thereby hiding the data message.

where

$$s(t) = \sum_{k=0}^{N-1} s_k \exp(j2\pi f_k t) = s_I(t) + js_Q(t), \quad (3)$$

with $s_k = d_k e^{j\theta_k}$ being the complex data symbols that are modulated onto the OFDM subcarriers and $f_k = f_b + k\Delta f$. Here f_b is the base frequency, Δf is the subcarrier spacing, and N is the total number of subcarriers. These parameters are appropriately selected so that the bandwidth of this OFDM signal matches the notch bandwidth in $X_N(t)$.

The above OFDM signal is inserted within the notched band-limited noise signal, with appropriate power matching, to produce the multi-functional Noise-OFDM radar transmit waveform, which is propagated by an omni-directional transmit antenna. As seen by any unintended receiver, the transmitted composite waveform clearly appears random and noise-like [4], preserving its covertness properties and hence presenting physical layer security. However, for other friendly radar sensors in the transmitting radar's vicinity, the waveform is construed as data plus noise. We show four different power spectrum plots in Fig. 2(a)-2(d) to demonstrate that the transmitted signal does appear noise-like to the outside observer and its OSA behavior.

B. Receive Component

In this work, we assume a time-invariant additive white Gaussian noise (AWGN) channel, ignoring the effects of varying channel response, carrier-frequency offsets, and I/Q imbalance at the OFDM receiver. Due to the omni-directional nature of the transmit antenna and its relatively high transmit power, the Noise-OFDM data signal is likely to be picked up by several radar sensors in the neighborhood of the transmitting radar. These radar sensors process this signal within their communication-receiver-subsystem, to retrieve the concealed digital data following OFDM demodulation, decoding, and detection. The composite Noise-OFDM transmit signal also travels to the target within the radar's range and returns as target backscatter. In the transmitting radar, this echo is processed by the radar-receiver-subsystem. Herein, the echo is cross-correlated with a time-delayed replica of the transmit Noise-OFDM waveform. The correlator maximizes the output signal-to-noise ratio (SNR) and hence helps in determining the range to the target.

III. PHYSICAL LAYER COEXISTENCE

To establish coexistence of communications with radar transmissions, the receive component must be analyzed further to answer two essential issues: 1) Effect on communications performance due to the presence of UWB noise around the OFDM signal? And 2) Effect on the radar's range and Doppler estimation capabilities due to the presence of an OFDM spectrum embedded inside the UWB random noise transmit spectrum?

A. Noise-embedded-communications Performance

Bit error rate (BER) is one of the most-widely used metrics for gauging the reliability of a communication technique. For the Noise-OFDM Radar, reliability depends on various parameters: the signal-to-noise ratio (SNR) at the input of the receiving antenna, the number of data subcarriers used, power difference between the notched noise signal and OFDM signal, and the BPF characteristics. The SNR at the input of the receiving antenna is defined as the ratio of the transmitted Noise-OFDM signal to the band-pass undesired channel noise received by the antenna. The general bit-error-rate of the Noise-OFDM Radar's communication subsystem has been derived to be [4]:

$$P_b = \frac{1}{N} \sum_{l=-\frac{N}{2}}^{l=\frac{N}{2}} P_b(Y_l) = \frac{1}{N} \sum_{l=-\frac{N}{2}}^{l=\frac{N}{2}} Q\left(\sqrt{\frac{\nu_l^2 \epsilon_{s,l}}{\sigma_{y,l}^2}}\right), \quad (4)$$

where the received signal on the l^{th} sub-carrier is Y_l , $\epsilon_{s,l}$ is the signal energy of the symbol being modulated onto the l^{th} OFDM sub-carrier, ν_l is the FIR filter response's magnitude ripple coefficient affecting the l^{th} OFDM sub-carrier and the additive white Gaussian noise has a variance $\sigma_{y,l}^2$ on the l^{th} OFDM sub-carrier. The perfect match of (4) with simulation results has been shown in [4]. We mention it here though, as it validates the multi-user BER vs. SNR simulations.

B. Target Detection Performance

In this sub-section, we examine the radar side of the coexisting system. The UWB noise radar is especially known for its high range resolution and good velocity resolution capabilities [10]. Range resolution states the capability of the radar to distinguish between two closely-separated targets. For a 1 GHz UWB noise radar, this implies that targets with 15 cm distance between one another will be correctly detected. And velocity resolution is the radar's capability of correctly estimating the speed of different moving targets, whose velocities are closely-separated. Noting the fact that we modified the transmit waveform of a typical noise radar to embed a communication signal inside it, we investigate the UWB Noise-OFDM radar's range and velocity resolution performance by formulating its AF. For random noise radar, since its output is a random function of time, only its statistics can be described. Therefore, an analogous ambiguity function may be defined as the expected value of the response of the correlator matched to a target at a desired range moving at

a desired velocity, to the return signal from the target at a different range moving at a different velocity. Consider the composite noise-OFDM signal reflected from a point target moving with constant velocity v_o at an instantaneous range of $R = R_o - v_o t$, with resulting delay $\tau_o = 2R_o/(c - v_o) \cong 2R_o/c$, and delay rate $\alpha = 2v_o/(c - v_o) \cong 2v_o/c$ such that $\tau(t) = \tau_o - 2v_o t/c = \tau_o - \alpha t$.

For conventional radars, the transmit signal envelope is of a deterministic nature for which a matched filter can be realized, and the time-invariant ambiguity function formulation establishes its range and velocity resolution properties. However, for a random noise radar, a matched filter cannot be realized; instead a correlator matched to the transmit process is required. Since its output is a random function of time, only its statistics can be described. Therefore, an analogous ambiguity function may be defined as the expected value of the response of the correlator matched to a target at a desired range moving at a desired velocity, to the return signal from the target at a different range moving at a different velocity. To discuss the range and Doppler resolution issues pertaining to the UWB Noise-OFDM Radar, we derive its generalized wideband ambiguity function as follows.

The received target backscatter at the radar in response to

Fig. 3. UWB Noise-OFDM Radar Sensor: Receive Component Architecture.

the transmitted signal can be expressed as

$$X_r(t) = k_1 X((1 + \alpha)t - \tau_o), \quad (5)$$

where k_1 is the arbitrary amplitude constant representing target cross-section, antenna pattern, propagation factors etc.

As shown in Fig. 3, the transmitted signal is passed through a delay line with time delay equal to τ_d and fed into one input of an up-converter MXR1. A local oscillator at f_{IF} also feeds into MXR1. Hence, the frequency shifted and time-delayed output is

$$X_d(t) = \frac{1}{4} [u(t - \tau_d) \exp(j\theta_1) + u^*(t - \tau_d) \exp(-j\theta_1)] - \frac{1}{4} [v(t - \tau_d) \exp(j\theta_2) + v^*(t - \tau_d) \exp(-j\theta_2)] + \frac{1}{4} [s(t - \tau_d) \exp(j\theta_2) + s^*(t - \tau_d) \exp(-j\theta_2)], \quad (6)$$

where $\theta_1 = 2\pi[(f_o - f_{IF})t - f_o\tau_d]$ and $\theta_2 = 2\pi[(f_n - f_{IF})t - f_n\tau_d]$.

System noise, assumed to be AWGN, is distributed on the complex envelopes of the components of X_r , X_d and is denoted by $|u_i, v_i, s_i|_{i=1,2}$. Now, passing signals X_r and

X_d through mixer MXR2, filtering through the IF BPF and dropping higher-order terms, the output can be shown to be:

$$Z_{IF} = \frac{1}{2} \{ \text{Real} [A_{IF} + B_{IF}] \}, \quad (7)$$

where

$$\begin{aligned} A_{IF} &= (u_1 u_2^*) \exp(-j2\pi(f_{IF}t + \alpha f_o t + f_o(\tau_d - \tau_o))) \\ B_{IF} &= (v_1 v_2^* + s_1 s_2^* + v_1 s_2^* + s_1 v_2^*) \\ &\quad \exp(-j2\pi(f_{IF}t + \alpha f_n t + f_n(\tau_d - \tau_o))). \end{aligned}$$

This Z_{IF} is then passed through the I/Q integrating filters with impulse response $h(t)$. The filter impulse response $h(t)$ could be of any type; however, in this analysis, we assume a rectangular time window for the filter response of the form

$$h(t) = 1/T, \text{ for } 0 \leq t \leq T; 0, \text{ otherwise.} \quad (8)$$

To estimate Z_{IF} , we evaluate $u_1 u_2^*$, $v_1 v_2^*$, $s_1 s_2^*$, $v_1 s_2^*$ and $s_1 v_2^*$ individually and take the expectation, which results in:

$$\begin{aligned} E\{u_1 u_2^*\} &= \{R_{cc}(\alpha t - \tau) - jR_{cs}(\alpha t - \tau)\} \\ E\{v_1 v_2^*\} &= \{R_{ccn}(\alpha t - \tau) - jR_{csn}(\alpha t - \tau)\} \\ E\{v_1 s_2^*\} &= E\{s_1 v_2^*\} = 0, \end{aligned} \quad (9)$$

where

$$R_{cc}(\cdot) = \frac{\sin[\pi\beta(\alpha t - \tau)]}{\pi\beta(\alpha t - \tau)}; \quad R_{ccn}(\cdot) = \frac{\sin[\pi\beta_n(\alpha t - \tau)]}{\pi\beta_n(\alpha t - \tau)} \quad (10)$$

are the system auto-correlation functions.

For evaluating $s_1 s_2^*$, we reasonably assume that identical data are transmitted over all sub-carriers of the OFDM symbol. We then use the orthogonality principle for OFDM carriers and equation (3) together, to finally show that $E\{s_1 s_2^*\} = NT_s$, where T_s is the symbol period.

Neglecting the phase terms, the expected values of the I and Q outputs of the I/Q integrating filters can therefore be symbolized as $\langle Z_I(\alpha, \tau, t) \rangle$ and $\langle Z_Q(\alpha, \tau, t) \rangle$.

Since the envelope of the output is defined to be the RMS sum of these two, the ambiguity function is of the form:

$$|\langle \chi(\alpha, \tau, t) \rangle| = \left[\langle Z_I \rangle^2 + \langle Z_Q \rangle^2 \right]^{1/2}. \quad (11)$$

Similar to [10], we go through the algebra of finding $\langle Z_I \rangle$ and $\langle Z_Q \rangle$, squaring and summing them, and use trigonometric identities to solve for equation (11). Ignoring the cross-correlation component due to the UWB noise as well as the notch spectrum (which is very low, hence negligible for a more uniform transmit PSD), equation (11) then reduces to the following simplified expression, which is the ambiguity function of a UWB Noise-OFDM Radar:

$$|\langle \chi(\alpha, \tau, t) \rangle| = |(A + B) \otimes h(t)|, \quad (12)$$

where

$$\begin{aligned} A &= R_{cc}(\alpha t - \tau) \exp(-j2\pi\alpha f_o t) \\ B &= (R_{ccn}(\alpha t - \tau) + NT_s) \exp(-j2\pi\alpha f_n t). \end{aligned} \quad (13)$$

The significance of this result, as drawn from our simulations in Section IV, is that the OFDM data bandwidth can be around 30% without adversely affecting ranging or Doppler estimation performance, noise-like properties of the radar.

IV. SIMULATION RESULTS

To validate the concepts mentioned above, we used MATLAB as the simulation platform. With f_1 , f_2 and f_n the same, a 253-tap finite-impulse-response (FIR) equiripple band-pass filter with a transition region bandwidth of ≈ 50 MHz and a pass-band magnitude ripple of ± 0.5 dB was used in the receiver. The input parameters were the number of subcarriers being used (which was 32 to cover a 100 MHz notch), the number of symbols per carrier (50 in our case), the bin length (1024), sample frequency (5 GHz) and the channel SNR. Based on this required channel SNR, appropriate noise power was added to the transmitted signal.

A. Multi-user Radar-Communications Performance

To study the multi-user BER vs. SNR characteristics of the Noise-OFDM radar, consider a multi-radar system where a radar i has neighbors j and k . We assume that i is allowed to communicate with j on the odd-numbered subcarriers, and with k on the even-numbered subcarriers respectively. Both j and k individually produce their transmit Noise-OFDM waveform and transmit it to i . Upon receiving their transmissions as a composite AWGN-affected waveform, i demodulates the incoming signal and separates j and k 's data bits. Fig. 4 shows the BER vs. SNR performance. Comparing Noise-OFDM to a pure OFDM signal, we observe that multi-user presence does quite heavily affect the noise-OFDM system, as can be seen from its high error-floor. However, utilizing a 3-carrier data redundancy technique (Noise-OFDM with data redundancy (DR)) as in [4], we see that this floor can be completely removed and the performance remarkably improves. Our system is able to achieve a BER better than 1×10^{-4} for an SNR of 9 dB. For this same BER, there is still an 8-dB difference though, from pure OFDM's performance. It is preferable to maintain this gap, as it is the price that we pay to achieve the PHY security that this system presents [4] to the transmit waveform.

Fig. 4. Noise-OFDM radar multi-user performance in AWGN channel.

B. Radar Operations

Target ranging, Doppler estimation, range resolution and Doppler resolution are the important metrics for measuring the performance of UWB noise radar. It was already shown in [4], that the range estimation performance of the UWB

Fig. 5. AF for a (a) UWB Noise Radar of 1 to 2 GHz, [10], (b) Noise-OFDM Radar with 300 MHz notch bandwidth.

Fig. 6. For $\alpha = 0$, the 2-D AF plot showing range resolution.

Noise-OFDM radar is unaffected by the presence of an OFDM signal in the transmit waveform. In this paper, for further verifying radar performance in the OSA presence of embedded communications, we simulated the AF expressed in equation (12). From the AF plot, range and Doppler resolution can be inferred, since range resolution $\Delta R = cT/2$, where $c = 3 \times 10^8$ m/s, and $T = 1/\text{bandwidth}$ is the first zero-crossing of the AF along τ axis. We used an integration time of 50 ms, a notch bandwidth of 300 MHz, and a center frequency of 1.45 GHz. The squared outcome (reduces side-lobes) of the convolution in equation (8) at time $t = T$ was stored for each α and τ . The resulting AF and its slice along τ axis is plotted in Fig. 5-(b) and Fig. 6, respectively. From Fig. 5-(b), it can be noted that the main lobe width (proportional to range resolution) remains relatively same as compared to a conventional UWB Noise Radar's AF main lobe in Fig. 5-(a) [10], although its side lobes are slightly higher. Fig. 6 in further detail, compares the range resolution of a UWB Noise Radar with a UWB Noise-OFDM Radar of varying notch bandwidths. Since our OSA goal is to have concealed coexistence of data with radar, we observe that a reasonable tradeoff can be reached between efficient wireless communications and covert radar operations: for e.g. as seen in Fig. 6, 300 MHz (30%) communications bandwidth is available with 45 cm radar range resolution in the UWB Noise-OFDM radar compared to 15 cm range resolution of conventional UWB Noise radar with no communications ability. It is also seen that range resolution gets better as the notch bandwidth (embedded OFDM bandwidth) is increased i.e., 15 cm for 900 MHz notch. However, as the embedded OFDM bandwidth increases, the overall noise-like behavior of the signal decreases [4], hence reducing its covertness.

Furthermore, a slice of Fig. 5-(b) along the α axis, showed that the Doppler resolution inferred as above, but along the α axis, does not change with the varying sizes of the notch bandwidth. This is as expected since the velocity resolution only depends on the integration time [10] and not on the waveform bandwidth. Therefore, with a 30% notch we are able to maintain the UWB noise radar's covertness and target resolution, while simultaneously using a portion of its bandwidth for communication.

V. CONCLUSIONS

In this work, we present a unique *covert opportunistic spectrum access solution* to enable the coexistence of OFDM-based data communications with UWB noise radars (the primary user). Using the same multi-functional composite waveform, we have demonstrated that reliable multi-user data transmission/reception can occur simultaneously with high resolution target detection/ranging. Towards this we also formulated the ambiguity function of this multi-functional waveform and have shown that around 30% of a 1 GHz UWB bandwidth is available for data communications, without adversely affecting the primary function of the radar. Promising and prospective candidates for implementing this system are Software Defined Radio (SDR) techniques of software-based signal processing, hardware such as the Universal Software Radio Peripheral (USRP) and high-speed digital-to-analog (DAC) converters. This will allow the system parameters to be software configurable, hence making an effective solution to dynamic spectrum access in first-emergency networks.

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